



$$[4] \Delta = \frac{n_1 - n_2}{n_1} \Rightarrow 1 - \frac{n_2}{n_1} = 0.01$$

$$n_2 = 0.99n_1 = 1.445$$

$$\sin \theta_c = \frac{n_2}{n_1} = \frac{1.445}{1.46} \Rightarrow \theta_c = 81.89^\circ$$

$$\sin \theta_{imax} = n_1 \sqrt{2\Delta} = 1.445 \sqrt{2(0.01)} \Rightarrow \theta_{imax} = 11.79^\circ$$

$$NA = n_a \sin \theta_{imax} = 0.209$$

$$[5] \Delta = \frac{(NA)^2}{2n_1^2} = \frac{(0.21)^2}{2(1.448)^2} = 0.0105$$

$$0.0105 = \frac{n_1 - n_2}{n_1} = \frac{1.448 - n_2}{1.448} \Rightarrow n_2 = 1.433$$

$$[6] NA = n_a \sin \theta_{imax} \Rightarrow 0.2 = 1.33 \sin \theta_{imax}$$

$$\theta_{imax} = \sin^{-1} \frac{0.2}{1.33} = 8.65^\circ$$

$$n_a \sin \theta_{imax} = n_1 \cos \theta_c$$

$$\frac{n_a \sin \theta_{imax}}{\sin \theta_c} = \frac{n_1}{\tan \theta_c}$$

$$\frac{n_a \sin \theta_{imax}}{\frac{n_2}{n_1}} = \frac{n_1}{\tan \theta_c} \Rightarrow \tan \theta_c = \frac{n_2}{NA}$$

$$\theta_c = \tan^{-1} \frac{1.59}{0.2} = 82.83^\circ$$

$$\sin \theta_c = \frac{n_2}{n_1} \Rightarrow n_1 = 1.6025$$

$$NA = \sqrt{n_1^2 - n_2^2} \approx 0.2 \text{ as given}$$

[7] (HW) Solve it by your self

[8] Condition of single mode

$$V = \frac{2\pi a}{\lambda} NA \leq 2.405$$

$$NA = \sqrt{n_1^2 - n_2^2} = 0.1316$$

$$\therefore \lambda \geq \frac{2\pi a}{V} NA \geq 1.375 \mu m$$

[9]  $\Delta = \frac{n_1 - n_2}{n_1} \Rightarrow 1 - \frac{n_2}{n_1} = 0.01$

$$n_2 = 0.99n_1 = 1.445$$

$$NA = n_1 \sqrt{2\Delta} = 1.46 \sqrt{2(0.01)} = 0.206$$

Condition of single mode

$$V = \frac{2\pi a}{\lambda} NA \leq 2.405$$

$$V_{max} = \frac{2\pi a}{\lambda_{min}} NA = \frac{2\pi a f_{max}}{c} NA = 2.405$$

$$f_{max} = 1.112 \times 10^{14} \text{ Hz}$$

[10]  $n_1 = 1.5, \alpha = 1.9, \Delta = 1.3\%, 2a = 40 \mu m, \lambda = 1.55 \mu m$

$$V = \frac{2\pi a}{\lambda} NA = \frac{2\pi a}{\lambda} (n_1 \sqrt{2\Delta})$$

$$V = \frac{2\pi(20 \times 10^{-6})}{1.55 \times 10^{-6}} \times 1.5 \times \sqrt{2(0.013)} = 19.6$$

$$M_{GI} = M_{SI} \left( \frac{\alpha}{\alpha + 2} \right)$$

$$M_{GI} = \frac{V^2}{4} = 96$$

Condition of single mode

$$V_c = 2.405 \left(1 + \frac{2}{\alpha}\right)^{\frac{1}{2}}$$

$$V_c = 3.4456$$

$$[11] \quad V = \frac{2\pi a}{\lambda} NA = \frac{2\pi a}{\lambda} (n_1 \sqrt{2\Delta}) = 75.8$$

$$M = \frac{V^2}{2} = 2873$$

$$a = \frac{\lambda V}{2\pi(n_1 \sqrt{2\Delta})} = \frac{2.405 \times 0.85 \times 10^{-6}}{2\pi(1.48\sqrt{2(0.015)})} = 1.27\mu\text{m}$$

After reduction of  $\Delta$  10 times

$$a = \frac{\lambda V}{2\pi(n_1 \sqrt{2\Delta})} = \frac{2.405 \times 0.85 \times 10^{-6}}{2\pi(1.48\sqrt{2(0.0015)})} = 4\mu\text{m}$$

[12] (HW) Solve it by your self.

**Good Luck**

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